



# Python

## Modul math

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# Modul `math`

Matematické funkce u Pythonu mogu se koristiti uz prethodnu najavu.

Te se naredbe nalaze u datoteci imena `math.py`.

Naredbe učitavamo u programski kod naredbom *`from math import *`*.

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016, 08:06:12) [MSC v.1900
D64] on win32
Type "copyright", "credits" or "license()" for more information.
>>> from math import *
>>> |
```



Funkcija **sqrt(x)** vraća realni broj koji predstavlja drugi korijen iz pozitivnog realnog broja x.

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016, 08:06:12) [MSC v.1900
D64] on win32
Type "copyright", "credits" or "license()" for more information.
>>> from math import *
>>> sqrt(16)
4.0
>>> sqrt(3)
1.7320508075688772
>>> sqrt(153.654)
12.39572506955523
>>> sqrt(-153.654)
Traceback (most recent call last):
  File "<pyshell#4>", line 1, in <module>
    sqrt(-153.654)
ValueError: math domain error
>>>
```




Funkcija **pow(x,y)** vraća realni broj koji predstavlja potenciju realnog broja x na realni broj y.

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016, 08:06:12) [MSC v.1900
D64] on win32
Type "copyright", "credits" or "license()" for more information.
>>> pow(2,3)
8
>>> pow(2,10)
1024
>>> pow(2.3,10.7)
7421.434270594758
>>> |
```



Funkcija **trunc(x)** vraća prirodni broj koji je jednak cijelomu dijelu realnog broja x.

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016, 08:06:12) [MSC v.1900
D64] on win32
Type "copyright", "credits" or "license()" for more information.
>>> from math import *
>>> trunc(16.456789)
16
>>> trunc(16.4)
16
>>> trunc(16)
16
>>> |
```



# Vrijednost **pi** unaprijed je definirana.

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016, 08:06:12) [MSC v.1900
D64] on win32
Type "copyright", "credits" or "license()" for more information.
>>> from math import *
>>> pi
3.141592653589793
>>> PI
Traceback (most recent call last):
  File "<pyshell#2>", line 1, in <module>
    PI
NameError: name 'PI' is not defined
>>> Pi
Traceback (most recent call last):
  File "<pyshell#3>", line 1, in <module>
    Pi
NameError: name 'Pi' is not defined
>>> # ispis većeg broja decimala broja pi
>>> print('%0.25f' % (pi))
3.1415926535897931159979635
>>> print('%0.50f' % (pi))
3.14159265358979311599796346854418516159057617187500
>>> |
```



# Funkcije $\sin(x)$ , $\cos(x)$ , $\tan(x)$ , $\text{atan}(x)$

```
Python 3.6.0 Shell
File Edit Shell Debug Options Window Help
Python 3.6.0 (v3.6.0:41df79263a11, Dec 23 2016,
06:12) [MSC v.1900 64 bit (AMD64)] on win32
Type "copyright", "credits" or "license()" for
information.
>>> from math import *
>>> sin(30)
-0.9880316240928618
>>> # računa sin od x u radijanima
>>> sin(radians(30))
0.49999999999999994
>>> cos(45)
0.5253219888177297
>>> cos(radians(45))
0.7071067811865476
>>> tan(56)
-0.6112736881917098
>>> tan(radians(56))
1.4825609685127403
>>> atan(-0.6112736881917098)
-0.5486677646162783
>>>
```



## 9.2.3. Trigonometric functions

```
math.acos(x)
Return the arc cosine of x, in radians.

math.asin(x)
Return the arc sine of x, in radians.

math.atan(x)
Return the arc tangent of x, in radians.

math.atan2(y, x)
Return atan(y / x), in radians. The result is between -pi and pi. The vector in the plane from the origin
to point (x, y) makes this angle with the positive X axis. The point of atan2() is that the signs of both
inputs are known to it, so it can compute the correct quadrant for the angle. For example, atan(1) and
atan2(1, 1) are both pi/4, but atan2(-1, -1) is -3*pi/4.

math.cos(x)
Return the cosine of x radians.

math.hypot(x, y)
Return the Euclidean norm, sqrt(x*x + y*y). This is the length of the vector from the origin to point (x, y).

math.sin(x)
Return the sine of x radians.

math.tan(x)
Return the tangent of x radians.
```

## 9.2.4. Angular conversion

```
math.degrees(x)
Convert angle x from radians to degrees.

math.radians(x)
Convert angle x from degrees to radians.
```

# Izračunaj pomoću trigonometrijskih funkcija

**sin**

```
>>> sin(radians(37))  
0.6018150231520483  
>>>  
>>> degrees(asin(0.6018150231520483))  
37.0
```

**cos**

```
>>> cos(radians(74))  
0.27563735581699916  
>>> degrees(acos(0.27563735581699916))  
74.0  
>>>
```

**tan**

```
>>> tan(radians(123))  
-1.5398649638145827  
>>> degrees(atan(-1.5398649638145827))  
-57.0  
>>>
```

**atan2**

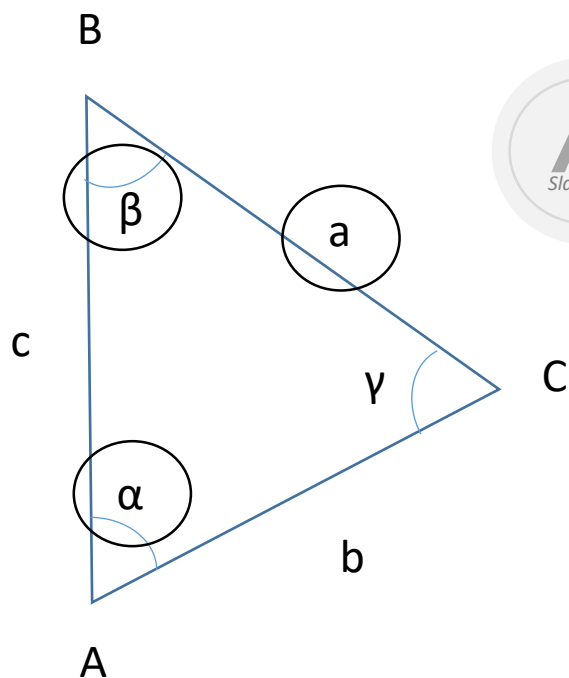
```
>>> degrees(atan2(45.12,23.69))  
62.29853627752536
```





# Računanje trokuta po sinusovom poučku

Napiši program u Pythonu koji će iz zadanih veličina izračunati stranice b i c.



**Zadatak 1.**  $\alpha = 40^\circ 33' 29''$   
 $\beta = 69^\circ 54' 22''$   
 $\gamma = 69^\circ 32' 07''$   
 $a = 230.25$

$$a : b = \sin \alpha : \sin \beta$$



$$b = (a \cdot \sin \beta) / \sin \alpha$$

$$a : c = \sin \alpha : \sin \gamma$$



$$c = (a \cdot \sin \gamma) / \sin \alpha$$

**Rješenje:**

$$b = 332.56$$

$$c = 331.76$$

**Zadatak 2.**

$$\alpha = 29^\circ 17' 02''$$

$$\beta = 56^\circ 56' 05''$$

$$\gamma = 93^\circ 46' 53''$$

$$a = 331.77$$

**Rješenje:**

$$b = 568.43$$

$$c = 676.80$$

**Zadatak 3.**

$$\alpha = 40^\circ 16' 29''$$

$$\beta = 85^\circ 33' 17''$$

$$\gamma = 54^\circ 10' 14''$$

$$a = 438.71$$

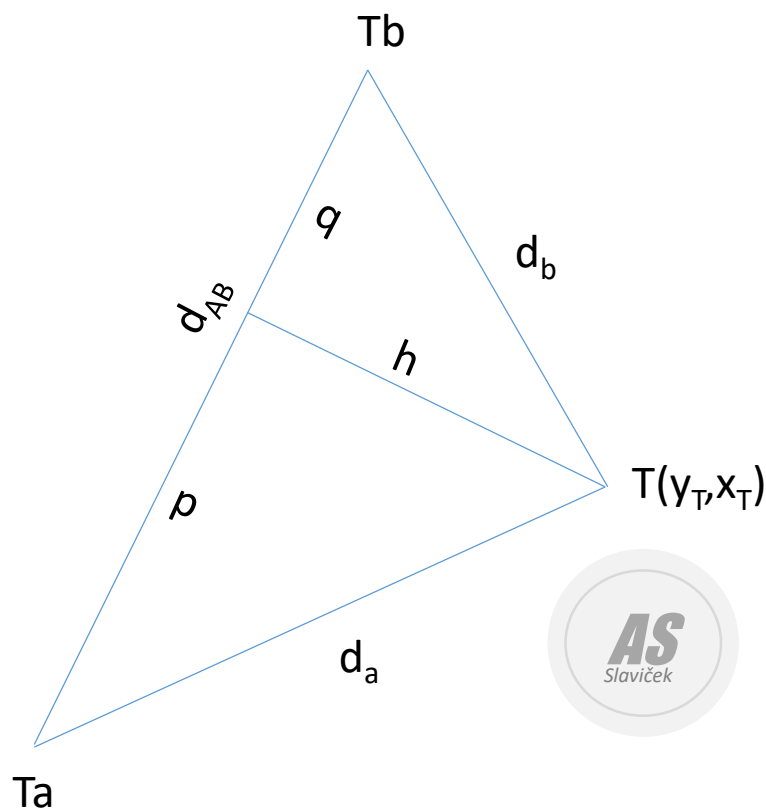
**Rješenje:**

$$b = 676.60$$

$$c = 550.22$$

# Trilateracija

(Lučni presjek)



```
# Točka T određena je lučnim presjekom, tj. odmjeranjem dužina da i db
# od točaka Ta i Tb čije su koordinate poznate.
# Unesi dužine: da i db.
# Unesi: Točka A(ya,xa,) i točke B(yb,xb)
# dy=yb-ya, dx=xb-xa
# dAB=sqrt(dy**2+dx**2)
# (a+b)/2=1/2 sqrt((yb-ya)**2+(xb-xa)**2)
# (a-b)/2=(da+db)*(da-db)/2dAB
# a= (a+b)/2+(a-b)/2
# b=(a+b)/2-(a-b)/2
# h=sqrt(da**2-a**2) ili sqrt(db**2-b**2)
# unesi predznak za h - za h je predznak pozitivan ako točka T leži
# lijevo od pravca TaTb, a negativan ako leži desno od njega
# p=(yb-ya)/(a+b)
# q=(xb-xa)/(a+b)
# yt=ya+a*p-h*q
# xt=xa+a*q+h*p
```

## LUČNI PRESJEK - PRIMJER

ya= 8116.03, xa= 2358.01

yb= 6942.00, xb= 1625.80

da= 755.77

db= 975.10

Točka se nalazi lijevo od pravca TaTb? Lijevo=1, Desno= -1 =-1

p= -0.8485042326072416

q = -0.5291885932704861

a= 554.638

b= 829.009

**yt = 7373.739**

**xt = 2500.112**

Napiši program u Pythonu koji će izračunati koordinate točke T.